

Generic Scalar Multiplication

Input: Integer k and generator G

Output: $P = kG$

$K = \text{Encode}(k)$

$S'_0 = \text{Init}(G)$

for K_i **in** $K = \{K_1, K_2, \dots, K_n\}$ **do**

$S_i = \text{Select}(S'_{i-1}, K_i)$

$S'_i = \text{Process}(S_i)$

$P = \text{Finalize}(S'_n)$

return P

- Secure Branches
- Table lookups
- Leakage free

- Point operations
- OTA target

Generic trace

An OTA assumes each execution of the `Process` operation leaks about the state S_i : $\text{Process}(S_i) \rightsquigarrow L_i(S_i)$. A generic trace is composed by a sequence of L_i : $\{L_1, L_2, \dots, L_n\}$.

Attack Input and Direction

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- "Projective coordinates attack" [2]: ≤ 5 bits
- **Backward OTA** (this): full scalar recovery.

Open Question:
how to get an intermediate state?

Controlled Side-Channels

Page	Instructions	Side-channels and their traces
P1	nop	PageTracer: Tracks the sequence of executed memory pages [4].
	nop	
	nop	
...	...	
P2	nop	CopyCat: Counts # executed instructions at each tracked page [5].
	...	
P3	nop	3
	nop	1
		2

Analyzed Open Source Libraries

libgcrypt

Double-and-add always

$R = \mathcal{O}$

for $i = \lfloor \log_2 k \rfloor$ **downto** 0 **do**

$R = 2R$

$T = R + G$

$R = \text{cond_assign}(T, R, k_i)$

return R

mbedtls

Comb method

$K = \text{Encode}(k)$

$P = \text{Precompute}(G)$

$R = \text{Select}(K_1, P)$

for $K_i \in K : i = [2, n]$ **do**

$R = 2R$

$T = \text{Select}(K_i, P)$

$R = R + T$

return R

wolfSSL

Montgomery ladder

$R = G, S = 2G$

for $i = \lfloor \log_2(k) \rfloor - 1$ **downto** 0 **do**

if $k_i = 0$ **then**

$S = R + S, R = 2R$

else

$R = R + S, S = 2S$

return R

Leakage Analysis

For each library we enumerated the memory pages used by the selected `Process` operations highlighted above. We evaluated the difficulty of an OTA for each memory page combination using both PageTracer and CopyCat side-channels. The percentages below correspond to the ratio of combinations that fall into **Ideal** and **Insecure** settings.

Attack	Ideal	Insecure	Max bias
PageTracer	0	87%	50%
CopyCat	50%	98%	30%

Attack	Ideal	Insecure	Max bias
PageTracer	84%	99%	62%
CopyCat	99%	100%	24%

Attack	Ideal	Insecure	Max bias
PageTracer	0	69%	52%
CopyCat	47%	94%	24%

References

- [1] Batina et al. **Online Template Attacks**. *INDOCRYPT*, 2014.
- [2] Naccache et al. **Projective Coordinates Leak**. *EUROCRYPT*, 2004.
- [3] Aldaya et al. **From A to Z: Projective Coordinates Leakage in the Wild**. *CHES*, 2020.
- [4] Xu et al. **Controlled-Channel Attacks: Deterministic Side Channels for Untrusted Operating Systems**. *IEEE Symposium on Security and Privacy*, 2015.
- [5] Moghimi et al. **CopyCat: Controlled Instruction-Level Attacks on Enclaves**. *USENIX Security Symposium*, 2020.
- [6] Dugardin et al. **Dismantling Real-World ECC with Horizontal and Vertical Template Attacks**. *COSADE*, 2016.



Paper



Demo

